



Department of Electrical Engineering and Computer Science

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

6.035 Fall
Test III

You have 50 minutes to finish this quiz.

Write your name and athena username on this cover sheet.

Some questions may be harder than others. Read them all through first and attack them in the order that allows you to make the most progress. If you find a question ambiguous, be sure to write down any assumptions you make. Be neat. If we can't understand your answer, we can't give you credit!

This exam is open book and open laptop. Additionally, you may access the course website, but aside from that you may NOT USE THE NETWORK.

Please do not write in the boxes below.

I (xx/??)	II (xx/??)	III (xx/??)	IV (xx/??)	Total (xx/??)

Name:

Athena username:

I Register Allocation

In this problem you will perform register allocation for the following Decaf program code. Note that each instruction is numbered. The functions `get_int()` and `printf()` are callout functions.

```
void main() {
    int x, y, z;

    1: x = get_int()
    2: y = get_int()
    3: while (x > 0) {
    4:   x = x - y;
      }
    5: z = x * y;
    6: if (z > -32) {
    7:   z = z - y;
      } else {
    8:   z = z + y;
      }
    9: printf (z);
}
```

1. [6 points]: Write the set of def-use chains for each variable in the program. Write each def-use chain as number pair (d, u) where d is the number of an instruction that defines the variable and u is the number of an instruction that uses that definition.

x :

y :

z :

2. [6 points]: Write the set of webs for each variable in the program. Write each web as the set of def-use chains that belong to the web. Label each web with a name, w_1, \dots, w_n .

x :

y :

z :

3. [6 points]: Draw the interference graph for the webs that you have identified. Specifically, each node in your graph should represent one web and there should be an edge between two nodes if the two webs interfere. Label each node with the name of the web it represents.

4. [6 points]: What is the minimum number of registers that we can use to store all variables without spilling? Justify your answer.

5. [3 points]: Assuming that you compile this Decaf program to the x86 architecture, which register would you select for the variable `z` to minimize the number of the generated assembly instructions?

6. [3 points]: Assuming that you compile this Decaf program to the x86 architecture, which register would you select for the variable `y` to minimize the number of the generated assembly instructions?

II Loop Identification and Induction Variables

Consider the following snippet of code (n is a constant, A is a global array; assume that the local variables are not used after the loops):

```
1:  i = 0; t0 = 0; t1 = 0; t2 = 0;
2:  while ( t0 < n ) {
3:      t0 = 2 * i + 1;
4:      for j = 0 to i {
5:          t1 = 2 * t0 + j;
6:          t2 = 7 * t1;
7:          A[i, j] = (j * t1) + t2;
8:      }
9:      if (t1 < 0) {
10:         t0 = t0 * t1;
11:     }
12:     i = i + 1;
13: }
```

7. [8 points]: Draw the control-flow graph and the dominator tree of this code side-by-side below. Mark the nodes that contain the statements with the corresponding numbers.

8. [2 points]: On the previous CFG, mark the header node of the outer loop with H0 and the header node of the inner loop with H1. Explain below why these nodes represent headers.

9. [5 points]: Identify the basic and the derived induction variables for the inner loop.

10. [5 points]: Is t_0 an induction variable in the outer loop? Explain why or why not. If not, is there a way to transform the program to make t_0 an induction variable?

11. [5 points]: Find a loop invariant code in either the inner or the outer loop. For each such piece of code, specify its line. Write below the optimized loop, after applying the loop-invariant code movement transformation.

12. [5 points]: Can we use the result of the induction variable analysis to perform strength reduction in the inner loop? If yes, write the optimized loop body. If no, explain why.

III Instruction Scheduling

Consider a simple machine that executes the instructions as follows:

- ALU instructions are executed within one clock cycle
- Memory load instructions are executed within two clock cycles
- Memory store instructions are executed within one clock cycle

Consider the following snippet of assembly code (we use local variables to represent stack locations):

```
1:   mov 0(%rbp), %r0
2:   mov -8(%rbp), %r1
3:   mul $3, %r0
4:   add %r0, %r1
5:   sub $1, %r0
6:   mov -16(%rbp), %r2
7:   add %r0, %r2
8:   mov %r1, -16(%rbp)
```

- 13. [7 points]:** Draw the dependence DAG for this code. Label each edge with the latency between the instructions.



14. [4 points]: Consider the machine with a single memory and a single ALU unit. Assume that the CPU executes without instruction scheduling. Fill in the table with the labels L1 to L8 for the instructions from the previous page that execute in each cycle. In how many cycles does the base execution complete?

	Clock													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Memory Unit														
ALU														

15. [7 points]: Consider the machine with a single memory and a single ALU unit. Use list scheduling algorithm to schedule the instructions and fill in the table below (use labels L1 to L8 for the corresponding instructions). What is the speedup compared to the base execution?

	Clock									
	1	2	3	4	5	6	7	8	9	10
Memory Unit										
ALU										

Speedup:

16. [7 points]: Consider now the machine with *two* stages memory unit (which can issue one memory operation in each cycle) and a single ALU unit. Use list scheduling algorithm to schedule the instructions and fill in the table below (use labels L1 to L8 for the corresponding instructions). What is the speedup compared to the base execution?

	Clock									
	1	2	3	4	5	6	7	8	9	10
Memory Unit 1										
Memory Unit 2										
ALU										

Speedup:

IV Loop Optimization

Consider the following loop (A is a global array, y and t are local variables, % is the modulo operator):

```
for i = 1 to n {  
    t = A[i] / A[i-1];  
    if ( i%2 == 1 ) { t = -t; }  
    y = y + t;  
}
```

17. [10 points]: Unroll the loop body two times. Write down the semantically equivalent unrolled loop (use BODY(J) to denote the three statements in the body of the loop for an induction variable J).

18. [5 points]: Outline the analysis and the transformation that would remove unnecessary if conditionals from the body of the unrolled loop.