### 6.006 Spring 2009

## Lecture 9: I ntroduction to Program Analysis and Optimization

## Outline

- Introduction
- Basic Blocks
- Common Subexpression Elimination
- Copy Propagation
- Dead Code Elimination
- Algebraic Simplification
- Summary


## Program Analysis

- Compile-time reasoning about run-time behavior of program
- Can discover things that are always true:
- " $x$ is always 1 in the statement $y=x+z$ "
- "the pointer p always points into array a"
- "the statement return 5 can never execute"
- Can infer things that are likely to be true:
- "the reference $r$ usually refers to an object of class C"
- "the statement $\mathrm{a}=\mathrm{b}+\mathrm{c}$ appears to execute more frequently than the statement $x=y+z^{\prime \prime}$
- Distinction between data and control-flow properties


## Transformations

- Use analysis results to transform program
- Overall goal: improve some aspect of program
- Traditional goals:
- Reduce number of executed instructions
- Reduce overall code size
- Other goals emerge as space becomes more complex
- Reduce number of cycles
- Use vector or DSP instructions
- Improve instruction or data cache hit rate
- Reduce power consumption
- Reduce memory usage


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## Control Flow Graph

- Nodes Represent Computation
- Each Node is a Basic Block
- Basic Block is a Sequence of Instructions with
- No Branches Out Of Middle of Basic Block
- No Branches Into Middle of Basic Block
- Basic Blocks should be maximal
- Execution of basic block starts with first instruction
- Includes all instructions in basic block
- Edges Represent Control Flow


## Control Flow Graph

into add(n, k) \{

$$
s=0 ; a=4 ; i=0 ;
$$

$$
\text { if }(k==0)
$$

$$
\mathrm{b}=1 ;
$$

else

$$
\text { b }-2 ;
$$

while ( $\mathrm{i}<\mathrm{n}$ ) \{

$$
\begin{aligned}
& s=s+a * b ; \\
& i=i+1 ;
\end{aligned}
$$

\}
return s;

$$
\begin{aligned}
& s=0 ; \\
& a=4 ; \\
& i=0 ; \\
& k==0
\end{aligned}
$$

\}

## Basic Block Construction

- Start with instruction control-flow graph
- Visit all edges in graph
- Merge adjacent nodes if
- Only one edge from first node
- Only one edge into second node

$$
\begin{gathered}
\hline s=0 ; \\
\square \\
a=4 ;
\end{gathered}
$$

$$
\square \quad \begin{aligned}
& \mathrm{s}=0 \\
& \mathrm{a}=4
\end{aligned}
$$














## Program Points, Split and J oin Points

- One program point before and after each statement in program
- Split point has multiple successors - conditional branch statements only split points
- Merge point has multiple predecessors
- Each basic block
- Either starts with a merge point or its predecessor ends with a split point
- Either ends with a split point or its successor starts with a merge point


## Basic Block Optimizations

- Common Sub

Expression Elimination

- $a=(x+y)+z ; b=x+y ;$
- $\mathrm{t}=\mathrm{x}+\mathrm{y}$; $\mathrm{a}=\mathrm{t}+\mathrm{z} ; \mathrm{b}=\mathrm{t}$;
- Constant Propagation
- $x=5 ; b=x+y ;$
- $x=5 ; b=5+y ;$
- Algebraic Identities
- $\quad \mathrm{a}=\mathrm{x}^{*} 1$;
- a=x;
- Copy Propagation
- $a=x+y ; b=a ; c=b+z ;$
- $a=x+y ; b=a ; c=a+z ;$
- Dead Code Elimination
- $a=x+y ; b=a ; b=a+z ;$
- $a=x+y ; \quad b=a+z$
- Strength Reduction
- t=i*4;
- $\mathrm{t}=\mathrm{i} \ll 2$;


## Basic Block Analysis Approach

- Assume normalized basic block - all statements are of the form
- var = var op var (where op is a binary operator)
- var $=$ op var (where op is a unary operator)
- var = var
- Simulate a symbolic execution of basic block
- Reason about values of variables (or other aspects of computation)
- Derive property of interest


## Two Kinds of Variables

- Temporaries Introduced By Compiler
- Transfer values only within basic block
- Introduced as part of instruction flattening
- Introduced by optimizations/transformations
- Typically assigned to only once
- Program Variables
- Declared in original program
- May be assigned to multiple times
- May transfer values between basic blocks


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## Value Numbering

- Reason about values of variables and expressions in the program
- Simulate execution of basic block
- Assign virtual value to each variable and expression
- Discovered property: which variables and expressions have the same value
- Standarduse:
- Common subexpression elimination
- Typically combined with transformation that
- Saves computed values in temporaries
- Replaces expressions with temporaries when value of expression previously computed


## New Basic

## Original Basic

 Block$$
\begin{aligned}
& a=x+y \\
& b=a+z \\
& b=b+y \\
& c=a+z
\end{aligned}
$$

Var to Val

$$
\begin{array}{lc}
x \rightarrow v 1 & \text { Exp to val } \\
\mathrm{y} \rightarrow \mathrm{v} 2 & \mathrm{v}+\mathrm{v} 2 \rightarrow \mathrm{v} 3 \\
\mathrm{a} \rightarrow \mathrm{v} 3 & \mathrm{v} 3+\mathrm{v} 4 \rightarrow \mathrm{v} \\
\mathrm{z} \rightarrow \mathrm{v} 4 & \mathrm{v} \\
\mathrm{~b} \rightarrow \mathrm{v} 6 & \mathrm{v} 2 \rightarrow \mathrm{v} 6
\end{array}
$$

Exp to Tmp $\mathrm{v} 1+\mathrm{v} 2 \rightarrow \mathrm{t} 1$ $\mathrm{v} 3+\mathrm{v} 4 \rightarrow \mathrm{t} 2$
$\mathrm{v} 5+\mathrm{v} 2 \rightarrow \mathrm{t} 6$

## Value Numbering Summary

- Forward symbolic execution of basic block
- Each new value assigned to temporary
- $a=x+y$; becomes $a=x+y$; $t=a ;$

Temporary preserves value for use later in program even if original variable rewritten

- $a=x+y ; \quad a=a+z ; b=x+y$ becomes
- $a=x+y ; t=a ; a=a+z ; b=t ;$
- Maps
- Var to Val - specifies symbolic value for each ${ }_{\text {var }}$ iable
- Exp to Val - specifies value of each evaluated expression
- Exp to Tmp - specifies tmp that holds value of each evaluated expression


## Map Usage

- Var to Val
- Used to compute symbolic value of $y$ and $z$ when processing statement of form $\mathrm{x}=\mathrm{y}+\mathrm{z}$
- Exp to Tmp
- Used to determine which tmp to use if value(y) + value(z) previously computed when processing statement of form $x-y+z$
- Exp to Val
- Used to update Var to Val when
- processing statement of the form $x=y+z$, and
- value(y) + value(z) previously computed


## Interesting Properties

- Finds common subexpressions even if they use different variables in expressions
- $\mathrm{y}=\mathrm{a}+\mathrm{b} ; \quad \mathrm{x}=\mathrm{b} ; \mathrm{z}=\mathrm{a}+\mathrm{x}$ becomes
$-\mathrm{y}=\mathrm{a}+\mathrm{b} ; \mathrm{t}=\mathrm{y}$; $\mathrm{x}=\mathrm{b} ; \mathrm{z}=\mathrm{t}$
- Why? Because computes with symbolic values
- Finds common subexpressions even if variable that originally held the value was overwritten
- $\mathrm{y}=\mathrm{a}+\mathrm{b} ; \quad \mathrm{y}=1 ; \mathrm{z}=\mathrm{a}+\mathrm{b}$ becomes
$-\mathrm{y}=\mathrm{a}+\mathrm{b} ; \mathrm{t}=\mathrm{y}$; $\mathrm{y}=1$; $\mathrm{z}=\mathrm{t}$
- Why? Because saves values away in temporaries


## One More Interesting Property

- Flattening and CSE combine to capture partial and arbitrarily complex common subexpressions

$$
\mathrm{w}=(\mathrm{a}+\mathrm{b})+\mathrm{c} ;
$$

$$
y=(a+x)+c ; z=a+b ;
$$

- After flattening:

$$
\mathrm{t} 1=\mathrm{a}+\mathrm{b} ; \mathrm{w}=\mathrm{t} 1+\mathrm{c} ; \quad \mathrm{x}=\mathrm{b} ; \mathrm{t} 2=\mathrm{a}+\mathrm{x} ; \mathrm{y}=\mathrm{t} 2+\mathrm{c} ; \quad \mathrm{z}=\mathrm{a}+\mathrm{b} ;
$$

- CSE algorithm notices that
- t1+c andt $2+\mathrm{c}$ compute same value
- In the statement $z=a+b, a+b$ has already been computed so generated code can reuse the result
$\mathrm{t} 1=\mathrm{a}+\mathrm{b} ; \mathrm{w}=\mathrm{t} 1+\mathrm{c} ; \mathrm{t} 3=\mathrm{w} ; \mathrm{x}=\mathrm{b} ; \mathrm{t} 2=\mathrm{t} 1 ; \mathrm{y}=\mathrm{t} 3 ; \quad \mathrm{z}=\mathrm{t} 1 ;$


## Problems I

- Algorithm has a temporary for each new value
- $\mathrm{a}=\mathrm{x}+\mathrm{y}$; $\mathrm{t} 1=\mathrm{a}$;
- I ntroduces
- lots of temporaries
- lots of copy statements to temporaries
- In many cases, temporaries and copy statements are unnecessary
- So we eliminate them with copy propagation and dead code elimination


## Problems II

- Expressions have to be identical
$-a=x+y+z ; b=y+z+x ; c=x^{*} 2+y+2 * z-(x+z)$
- We use canonicalization
- We use algebraic simplification


## Copy Propagation

- Once again, simulate execution of program
- If can, use original variable instead of temporary
- $a=x+y ; b=x+y ;$
- After CSE becomes $\mathrm{a}=\mathrm{x}+\mathrm{y}$; $\mathrm{t}=\mathrm{a}$; $\mathrm{b}=\mathrm{t}$;
- After CP becomes $a=x+y ; t=a ; b=a ;$
- After DCE becomes $\mathrm{a}=\mathrm{x}+\mathrm{y}$; $\mathrm{b}=\mathrm{a}$;
- Key idea:
- determine when original variable is NOT overwritten between its assignment statement and the use of the computed value
- If not overwritten, use original variable


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## Copy Propagation Maps

- Maintain two maps
- tmp to var: tells which variable to use instead of a given temporary variable
- var to set: inverse of tmp to var. tells which temps are mapped to a given variable by tmp to var


## Copy Propagation Example

- Original

$$
\begin{aligned}
& a=x+y \\
& b=a+z \\
& c=x+y \\
& a=b
\end{aligned}
$$

- After CSE

$$
\begin{aligned}
& \mathrm{a}=\mathrm{x}+\mathrm{y} \\
& \mathrm{t} 1=\mathrm{a} \\
& \mathrm{~b}=\mathrm{a}+\mathrm{z} \\
& \mathrm{t} 2=\mathrm{b} \\
& \mathrm{c}=\mathrm{t} 1 \\
& \mathrm{a}=\mathrm{b}
\end{aligned}
$$

- After CSE and Copy Propagation
$a=x+y$
$\mathrm{t} 1=\mathrm{a}$
$\mathrm{b}=\mathrm{a}+\mathrm{z}$
t2 $=$ b
$\mathrm{c}=\mathrm{a}$
$\mathrm{a}=\mathrm{b}$


## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a
\end{aligned}
$$

tmp to var
$\mathrm{t} 1 \rightarrow \mathrm{a}$
var to set

$$
a \rightarrow\{\mathrm{t} 1\}
$$

## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b
\end{aligned}
$$

tmp to var

$$
\begin{aligned}
& \mathrm{t} 1 \rightarrow \mathrm{a} \\
& \mathrm{t} 2 \rightarrow \mathrm{~b}
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b
\end{aligned}
$$

var to set

$$
\begin{aligned}
& \mathrm{a} \rightarrow\{\mathrm{t} 1\} \\
& \mathrm{b} \rightarrow\{\mathrm{t} 2\}
\end{aligned}
$$

## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=t 1
\end{aligned}
$$

tmp to var

$$
\begin{aligned}
& \mathrm{t} 1 \rightarrow \mathrm{a} \\
& \mathrm{t} 2 \rightarrow \mathrm{~b}
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b
\end{aligned}
$$

var to set

$$
\begin{aligned}
& \mathrm{a} \rightarrow\{\mathrm{t} 1\} \\
& \mathrm{b} \rightarrow\{\mathrm{t} 2\}
\end{aligned}
$$

## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=t 1
\end{aligned}
$$

tmp to var

$$
\begin{aligned}
& \mathrm{t} 1 \rightarrow \mathrm{a} \\
& \mathrm{t} 2 \rightarrow \mathrm{~b}
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& \mathrm{a}=\mathrm{x}+\mathrm{y} \\
& \mathrm{t} 1=\mathrm{a} \\
& \mathrm{~b}=\mathrm{a}+\mathrm{z} \\
& \mathrm{t} 2=\mathrm{b} \\
& \mathrm{c}=\mathrm{a}
\end{aligned}
$$

var to set

$$
\begin{aligned}
& \mathrm{a} \rightarrow\{\mathrm{t} 1\} \\
& \mathrm{b} \rightarrow\{\mathrm{t} 2\}
\end{aligned}
$$

## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=t 1 \\
& a=b
\end{aligned}
$$

tmp to var

$$
\begin{aligned}
& \mathrm{t} 1 \rightarrow \mathrm{a} \\
& \mathrm{t} 2 \rightarrow \mathrm{~b}
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& \mathrm{a}=\mathrm{x}+\mathrm{y} \\
& \mathrm{t} 1=\mathrm{a} \\
& \mathrm{~b}=\mathrm{a}+\mathrm{z} \\
& \mathrm{t} 2=\mathrm{b} \\
& \mathrm{c}=\mathrm{a} \\
& \mathrm{a}=\mathrm{b} \\
& \text { var to set } \\
& \mathrm{a} \rightarrow\{\mathrm{t} 1\} \\
& \mathrm{b} \rightarrow\{\mathrm{t} 2\}
\end{aligned}
$$

## Copy Propagation Example

Basic Block After CSE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=t 1 \\
& a=b
\end{aligned}
$$

tmp to var

$$
\begin{aligned}
& \mathrm{t} 1 \rightarrow \mathrm{t} 1 \\
& \mathrm{t} 2 \rightarrow \mathrm{~b}
\end{aligned}
$$

Basic Block After
CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=a \\
& a=b \\
& \text { var to set } \\
& a \rightarrow\} \\
& b \rightarrow\{t 2\}
\end{aligned}
$$

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## Dead Code Elimination

- Copy propagation keeps all temps around
- May be temps that are never read
- Dead Code Elimination removes them Basic Block After CSE and CP

Basic Block After CSE, CP and DCE

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
& c=a \\
& a=b
\end{aligned}
$$

$$
\begin{aligned}
& a=x+y \\
& b=a+z \\
& c=a \\
& a=b
\end{aligned}
$$

## Dead Code Elimination

- Basic Idea
- Process Code In Reverse Execution Order
- Maintain a set of variables that are needed later in computation
- If encounter an assignment to a temporary that is not needed, remove assignment


## Basic Block After <br> CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& \mathrm{t} 1=\mathrm{a} \\
& \mathrm{~b}=\mathrm{a}+\mathrm{z} \\
& \mathrm{t} 2=\mathrm{b} \\
& \mathrm{c}=\mathrm{a} \\
& \Rightarrow \mathrm{a}=\mathrm{b}
\end{aligned}
$$

Needed Set \{b\}

## Basic Block After <br> CSE and Copy Prop

$$
\begin{array}{ll} 
& a=x+y \\
& t 1=a \\
& b=a+z \\
& t 2=b \\
\Rightarrow & c=a \\
& a=b
\end{array}
$$

Needed Set

$$
\{a, b\}
$$

## Basic Block After <br> CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z \\
\Rightarrow & t 2=b \\
& c=a \\
& a=b
\end{aligned}
$$

Needed Set

$$
\{\mathrm{a}, \mathrm{~b}\}
$$

## Basic Block After <br> CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
& b=a+z
\end{aligned}
$$

$\longmapsto$

$$
\begin{aligned}
& c=a \\
& a=b
\end{aligned}
$$

Needed Set

$$
\{\mathrm{a}, \mathrm{~b}\}
$$

## Basic Block After <br> CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
& t 1=a \\
\Longrightarrow & b=a+z
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{c}=\mathrm{a} \\
& \mathrm{a}=\mathrm{b}
\end{aligned}
$$

Needed Set

$$
\{a, b, z\}
$$

## Basic Block After <br> CSE and Copy Prop

$$
\begin{aligned}
& a=x+y \\
t 1 & =a \\
b & =a+z \\
& \\
& =a \\
a & =b
\end{aligned}
$$

Needed Set

$$
\{a, b, z\}
$$

## Basic Block After <br> CSE and Copy Prop



$$
b=a+z
$$

$$
c=a
$$

$$
\mathrm{a}=\mathrm{b}
$$

Needed Set

$$
\{a, b, z\}
$$

## Basic Block After , CSE Copy Propagation, and Dead Code Elimination

$$
\Longrightarrow a=x+y
$$

$$
\begin{aligned}
& b=a+z \\
& c=a \\
& a=b
\end{aligned}
$$

Needed Set

$$
\{a, b, z\}
$$

## Basic Block After , CSE Copy Propagation, and Dead Code Elimination

$$
\begin{aligned}
& a=x+y \\
& b=a+z \\
& c=a \\
& a=b
\end{aligned}
$$

Needed Set

$$
\{a, b, z\}
$$

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## Algebraic Simplification

- Apply our knowledge from algebra, number theory etc. to simplify expressions


## Algebraic Simplification

- Apply our knowledge from algebra, number theory etc. to simplify expressions
- Example

$$
\begin{array}{ll}
-a+0 & \Rightarrow a \\
-a * 1 & \Rightarrow a \\
-a / 1 & \Rightarrow a \\
-a * 0 & \Rightarrow 0 \\
-0-a & \Rightarrow-a \\
-a+(-b) & \Rightarrow a-b \\
--(-a) & \Rightarrow a
\end{array}
$$

## Algebraic Simplification

- Apply our knowledge from algebra, number theory etc. to simplify expressions
- Example
$-a \wedge$ true $\quad \Rightarrow$ a
$-a \wedge$ false $\quad \Rightarrow$ false
$-a \vee$ true $\quad \Rightarrow$ true
- a $\vee$ false $\quad \Rightarrow$ a


## Algebraic Simplification

- Apply our knowledge from algebra, number theory etc. to simplify expressions
- Example

$$
\begin{array}{ll}
-a^{\wedge} 2 & \Rightarrow a * a \\
-a^{*} 2 & \Rightarrow a+a \\
-a^{*} 8 & \Rightarrow a \ll 3
\end{array}
$$

## Opportunities for Algebraic Simplification

- In the code
- Programmers are lazy to simplify expressions
- Programs are more readable with full expressions
- After compiler expansion
- Example: Array read A[8][12] will get expanded to
- *(Abase $\left.+4^{*}\left(12+8^{*} 256\right)\right)$ which can be simplified
- After other optimizations


## Usefulness of Algebraic Simplification

- Reduces the number of instructions
- Uses less expensive instructions
- Enable other optimizations


## I mplementation

- Not a data-flow optimization!
- Find candidates that matches the simplification rules and simplify the expression trees
- Candidates may not be obvious


## I mplementation

- Not a data-flow optimization!
- Find candidates that matches the simplification rules and simplify the expression trees
- Candidates may not be obvious
- Example $a+b \quad a$



## Use knowledge about operators

- Commutative operators
- a Op b = b Op a
- Associative operators
- (a op b) op c = b op (a op c)


## Canonical Format

- Put expression trees into a canonical format
- Sum of multiplicands
- Variables/terms in a canonical order
- Example $(a+3) *(a+8) * 4 \Rightarrow 4^{*} a * a+44^{*} a+96$
- Section 12.3.1 of whale book talks about this


## Effects on the Numerical Stability

- Some algebraic simplifications may produce incorrect results


## Effects on the Numerical Stability

- Some algebraic simplifications may produce incorrect results
- Example

$$
-(a / b) * 0+c
$$

## Effects on the Numerical Stability

- Some algebraic simplifications may produce incorrect results
- Example
- (a/b)*0 + c
- we can simplify this to c


## Effects on the Numerical Stability

- Some algebraic simplifications may produce incorrect results
- Example
- (a / b)*0 + c
- we can simplify this to c
- But what about when $b=0$ should be a exception, but we'll get a result!


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## Interesting Properties

- Analysis and Transformation Algorithms Symbolically Simulate Execution of Program
- CSE and Copy Propagation go forward
- Dead Code Elimination goes backwards
- Transformations stacked
- Group of basic transformations work together
- Often, one transformation creates inefficient code that is cleaned up by following transformations
- Transformations can be useful even if original code may not benefit from transformation


## Other Basic Block Transformations

- Constant Propagation
- Strength Reduction
$-a \ll 2=a * 4 ; a+a+a=3 * a ;$
- Do these in unified transformation framework, not in earlier or later phases


## Summary

- Basic block analyses and transformations
- Symbolically simulate execution of program
- Forward (CSE, copy prop, constant prop)
- Backward (Dead code elimination)
- Stacked groups of analyses and transformations that work together
- CSE introduces excess temporaries and copystatements
- Copy propagation often eliminates need to keep temporary variables around
- Dead code elimination removes useless code
- Similar in spirit to many analyses and transformations that operate across basic blocks

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