

Memory Optimization

Outline

- Issues with the Memory System
- Loop Transformations
- Data Transformations
- Prefetching
- Alias Analysis

Memory Hierarchy

1 - 2 ns	Registers	32 – 512 B
3 - 10 ns	L1 Private Cache	16 – 128 KB
8 - 30 ns	L2/L3 Shared Cache	1 – 16 MB
60 - 250 ns	Main Memory (DRAM)	1 GB – 128 GB
5 - 20 ms	Permanent Storage (Hard Disk)	250 GB – 4 TB

Processor-Memory Gap



Year

Cache Architecture

		Pentium D	Core Duo	Core 2 Duo	Athlon 64
L1 code (per core)	size	12 K uops	32 KB	32 KB	64 KB
	associativity	8 way	8 way	8 way	2 way
	Line size	64 bytes	64 bytes	64 bytes	64 bytes
L1 data (per core)	size	16 KB	32 KB	32 KB	64 KB
	associativity	8 way	8 way	8 way	8 way
	Line size	64 bytes	64 bytes	64 bytes	64 bytes
L1 to L2	Latency	4 cycles	3 cycles	3 cycles	3 cycles
L2 shared	size	4 MB	4 MB	4 MB	1 MB
	associativity	8 way	8 way	16 way	16 way
	Line size	64 bytes	64 bytes	64 bytes	64 bytes
L2 to L3(off)	Latency	31 cycles	14 cycles	14 cycles	20 cycles

Cache Misses

- Cold misses
 - First time a data is accessed
- Capacity misses
 - Data got evicted between accesses because a lot of other data (more than the cache size) was accessed
- Conflict misses
 - Data got evicted because a subsequent access fell on the same cache line (due to associativity)
- True sharing misses (multicores)
 - Another processor accessed the data between the accesses
- False sharing misses (multicores)
 - Another processor accessed different data in the same cache line between the accesses

Data Reuse

• Temporal Reuse

 A given reference accesses the same location in multiple iterations

Spatial Reuse

 Accesses to different locations within the same cache line

• Group Reuse

 Multiple references access the same location for i = 0 to N for j = 0 to N A[j] =

for i = 0 to N for j = 0 to N B[i, j] =

for i = 0 to N A[i] = A[i-1] + 1

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Matrix Multiply

```
for i = 1 to n
for j = 1 to n
for k = 1 to n
c[i,j] += a[i,k]*b[k,j]
```

Example: Matrix Multiply





Data Accessed

1,050,624

Matrix Multiply

for i0 = 1 to n step b for j0 = 1 to n step b for k0 = 1 to n step b for 1 = i0 to min(i0+b-1, n) for j = j0 to min(j0+b-1, n) for k = k0 to min(k0+b-1, n) c[i,j] += a[i,k]*b[k,j]

Example: Matrix Multiply







1,050,624



66,560

- Transform the iteration space to reduce the number of misses
- Reuse distance For a given access, number of other data items accessed before that data is accessed again
- Reuse distance > cache size
 - Data is spilled between accesses

Divide and Conquer Matrix Multiply



for i = 0 to N for j = 0 to N for k = 0 to N A[k,j]

Reuse distance = N^2

If Cache size < 16 doubles? A lot of capacity misses



for i = 0 to N for j = 0 to N for k = 0 to N A[k,j]Loop Interchange for j = 0 to N for i = 0 to N for k = 0 to N A[k,j]



for j = 0 to N for i = 0 to N for k = 0 to N A[k,j]

Cache line size > data size Cache line size = L Reuse distance = LN

If cache size < 8 doubles? Again a lot of capacity misses



for j = 0 to N for i = 0 to N for k = 0 to N A[k,j]Loop Interchange for k = 0 to N for i = 0 to N

for f = 0 to N for f = 0 to N A[k,j]



for i = 0 to N for j = 0 to N for k = 0 to N A[i,j] = A[i,j] + B[i,k] + C[k,j]

• No matter what loop transformation you do one array access has to traverse the full array multiple times

Loop Tiling

for i = 0 to N for j = 0 to N

for ii = 0 to ceil(N/b)
for jj = 0 to ceil(N/b)
for i = b*ii to min(b*ii+b-1, N)
for j = b*jj to min(b*jj+b-1, N)





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False Sharing Misses

for J = forall I = X(I, J) = ...





Conflict Misses

for J = forall I = X(I, J) = ...





Array X

Data Transformations

Similar to loop transformations

All the accesses have to be updated
 Whole program analysis is required



	Strip-Minding Create two dims from one	Permutation Change memory layout		
	With blocksize=4	With permutation matrix $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$		
Storage Declaration	$\binom{N}{\frac{N}{4}}$	$\begin{bmatrix} N_1 \\ N_2 \end{bmatrix} \begin{bmatrix} N_2 \\ N_1 \end{bmatrix}$		
Array Access	<i>i</i> mod 4 <i>i</i> /4	$\begin{bmatrix} i_1 \\ i_2 \end{bmatrix} \begin{bmatrix} i_2 \\ i_1 \end{bmatrix}$		
Memory Layout	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		

Data Transformation Algorithm

- Rearrange data: Each processor's data is contiguous
- Use data decomposition
 - *, block, cyclic, block-cyclic
- Transform each dimension according to the decomposition
- Use a combination of strip-mining and permutation primitives

Example I: (Block, Block)

i₂

 i_{l}

 $\left[\begin{array}{c}i_1\\i_2\end{array}\right]$

Example I: (Block, Block)





 i_1

Example I: (Block, Block)



 i_1













 i_2

 i_1/P

Performance





1 2 4 4 6 8 10 12 16 18 20 22 24 26 28 30 32

- Parallelizing outer loop
- Best computation placement
- + data transformations

Optimizations

- Modulo and division operations in the index calculation
 - Very high overhead
- Use standard techniques
 - Loop invariant removal, CSE
 - Strength reduction exploiting properties of modulo and division
 - Use knowledge about the program

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Prefetching

- Cache miss stalls the processor for hundreds of cycles
 - Start fetching the data early so it'll be available when needed
- Pros
 - Reduction of cache misses \rightarrow increased performance
- Cons
 - Prefetch contents for fetch bandwidth
 - Solution: Hardware only issue prefetches on unused bandwidth
 - Evicts a data item that may be used
 - Solution: Don't prefetch too early
 - Pretech is still pending when the memory is accessed
 - Solution: Don't prefetch too late
 - Prefetch data is never used
 - Solution: Prefetch only data guaranteed to be used
 - Too many prefetch instructions
 - Prefetch only if access is going to miss in the cache

Prefetching

Compiler inserted

- Use reuse analysis to identify misses
- Partition the program and insert prefetches
- Run ahead thread (helper threads)
 - Create a separate thread that runs ahead of the main thread
 - Runahead only does computation needed for controlflow and address calculations
 - Runahead performs data (pre)fetches

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Alias Analysis

- Aliases destroy local reasoning
 - Simple, local transformations require global reasoning in the presence of aliases
 - A critical issue in pointer-heavy code
 - This problem is even worse for multithreaded programs

Two solutions

- Alias analysis
 - Tools to tell us the potential aliases
- Change the programming language
 - Languages have no facilities for talking about aliases
 - Want to make local reasoning possible



Definition *Two pointers that point to the same location* are **aliases**

Example

 Y = &Z
 X = Y
 X = 3 / changes the value of *Y */

Example

```
foo(int * A, int * B, int * C, int N)
for i = 0 to N-1
A[i]= A[i]+ B[i] + C[i]
```

- Is this loop parallel?
- Depends

int X[1000]; int Y[1000]; int Z[1000] foo(X, Y, Z, 1000); int X[1000]; foo(&X[1], &X[0], &X[2], 998);

Points-To Analysis

- Consider:
 - $\mathsf{P} = \& \mathsf{Q}$

$$Y = \&\bar{z}$$

- X = Y
- *X = P
- Informally:
 - P can point to Q
 - Y can point to Z
 - X can point to Z
 - Z can point to Q



Points-To Relations

• A graph

- Nodes are program names
- Edge (x,y) says x may point to y

Finite set of names

- Implies each name represents many heap cells
- Correctness: If *x = y in any state of any execution, then (x,y) is an edge in the points-to graph

Sensitivity

Context sensitivity

- Separate different uses of functions
- Different is the key if the analysis think the input is the same, reuse the old results

• Flow sensitivity

- For insensitivity makes any permutation of program statements gives same result
- Flow sensitive is similar to data-flow analysis

Conclusion

- Memory systems are designed to give a huge performance boost for "normal" operations
- The performance gap between good and bad memory usage is huge
- Programs analyses and transformations are needed
- Can off-load this task to the compiler